

Please check the examination details below before entering your candidate information

Candidate surname

Other names

Centre Number

Candidate Number

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## Pearson Edexcel Level 3 GCE

**Wednesday 14 June 2023**

Afternoon (Time: 1 hour 30 minutes)

Paper  
reference

**9FM0/3C**

### Further Mathematics

Advanced

**PAPER 3C: Further Mechanics 1**

**You must have:**

Mathematical Formulae and Statistical Tables (Green), calculator

Total Marks

**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

#### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear.  
Answers without working may not gain full credit.
- Unless otherwise indicated, whenever a value of  $g$  is required, take  $g = 9.8 \text{ m s}^{-2}$  and give your answer to either 2 significant figures or 3 significant figures.

#### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 7 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

#### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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1. A particle  $P$  of mass 2 kg is moving with velocity  $(-4\mathbf{i} + 3\mathbf{j})\text{ m s}^{-1}$  when it receives an impulse  $(-6\mathbf{i} + 42\mathbf{j})\text{ N s}$ .

(a) Find the speed of  $P$  immediately after receiving the impulse.

(4)

The angle through which the direction of motion of  $P$  has been deflected by the impulse is  $\alpha^\circ$

(b) Find the value of  $\alpha$

(2)





2. A car of mass 1000 kg moves in a straight line along a horizontal road at a constant speed  $U \text{ ms}^{-1}$ . The resistance to the motion of the car is a constant force of magnitude 400 N.

The engine of the car is working at a constant rate of 16 kW.

- (a) Find the value of  $U$ .

(3)

The car now pulls a trailer of mass 600 kg in a straight line along the road using a tow rope which is parallel to the direction of motion. The resistance to the motion of the car is again a constant force of magnitude 400 N. The resistance to the motion of the trailer is a constant force of magnitude 300 N.

The engine of the car is working at a constant rate of 16 kW.

The tow rope is modelled as being light and inextensible.

Using the model,

- (b) find the tension in the tow rope at the instant when the speed of the car is  $\frac{20}{3} \text{ ms}^{-1}$

(5)

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Question 2 continued

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3. A particle  $P$  of mass  $2m$  is moving in a straight line with speed  $3u$  on a smooth horizontal plane. It collides directly with a particle  $Q$  of mass  $m$  that is moving on the plane with speed  $2u$  in the opposite direction to  $P$ .

The coefficient of restitution between  $P$  and  $Q$  is  $e$ , where  $e > \frac{4}{5}$

- (a) Show that the speed of  $Q$  immediately after the collision is  $\frac{(4 + 10e)u}{3}$  (6)

After the collision  $Q$  hits a smooth fixed vertical wall that is perpendicular to the direction of motion of  $Q$ . The coefficient of restitution between  $Q$  and the wall is  $f$ .

- (b) Find, **in terms of  $e$** , the set of values of  $f$  for which there will be a second collision between  $P$  and  $Q$ . (4)

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**Question 3 continued**

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**(Total for Question 3 is 10 marks)**



4. A light elastic string has natural length  $2a$  and modulus of elasticity  $4mg$ .  
 One end of the elastic string is attached to a fixed point  $O$ . A particle  $P$  of mass  $m$  is attached to the other end of the elastic string.  
 The particle  $P$  hangs freely in equilibrium at the point  $E$ , which is vertically below  $O$

(a) Find the length  $OE$ . (4)

Particle  $P$  is now pulled vertically downwards to the point  $A$ , where  $OA = 4a$ , and released from rest. The resistance to the motion of  $P$  is a constant force of magnitude  $\frac{1}{4}mg$ .

(b) Find, in terms of  $a$  and  $g$ , the speed of  $P$  after it has moved a distance  $a$ . (7)

Particle  $P$  is now held at  $O$   
 Particle  $P$  is released from rest and reaches its maximum speed at the point  $B$ .

The resistance to the motion of  $P$  is again a constant force of magnitude  $\frac{1}{4}mg$ .

(c) Find the distance  $OB$ . (4)

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**Question 4 continued**

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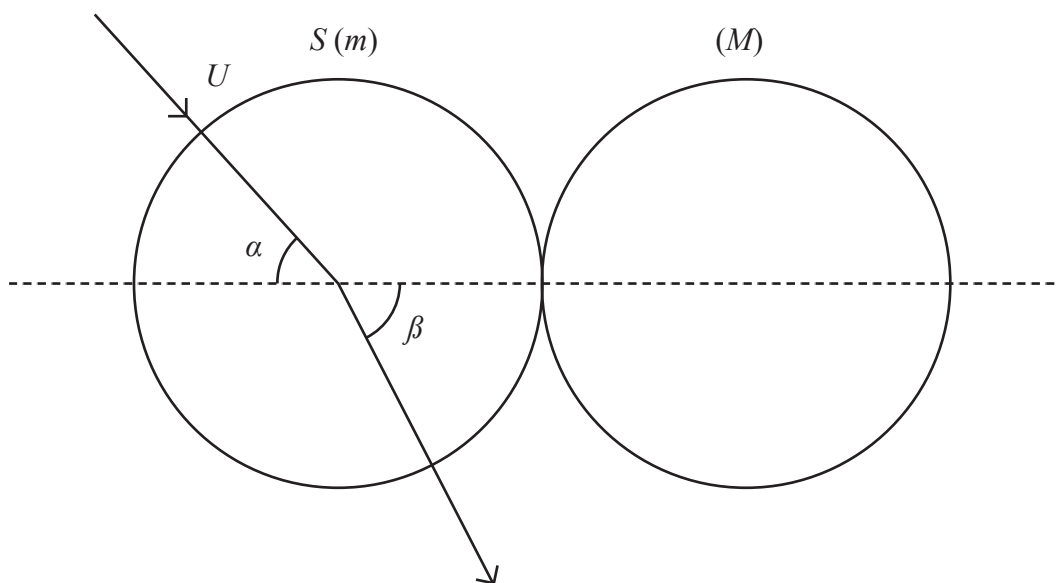


Figure 1

A smooth uniform sphere  $S$  of mass  $m$  is moving with speed  $U$  on a smooth horizontal plane. The sphere  $S$  collides obliquely with another uniform sphere of mass  $M$  which is at rest on the plane. The two spheres have the same radius.

Immediately before the collision the direction of motion of  $S$  makes an angle  $\alpha$ , where  $0 < \alpha < 90^\circ$ , with the line joining the centres of the spheres.

Immediately after the collision the direction of motion of  $S$  makes an angle  $\beta$  with the line joining the centres of the spheres, as shown in Figure 1.

The coefficient of restitution between the spheres is  $e$ .

(a) Show that  $\tan \beta = \frac{(m + M) \tan \alpha}{(m - eM)}$  (8)

Given that  $m = eM$ ,

(b) show that the directions of motion of the two spheres immediately after the collision are perpendicular. (2)

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Question 5 continued

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6. A particle  $P$  of mass  $m$  is falling vertically when it strikes a fixed smooth inclined plane. The plane is inclined to the horizontal at an angle  $\alpha$ , where  $0 < \alpha \leq 45^\circ$

At the instant immediately before the impact, the speed of  $P$  is  $u$ .

At the instant immediately after the impact,  $P$  is moving horizontally with speed  $v$ .

- (a) Show that the magnitude of the impulse exerted on the plane by  $P$  is  $mu \sec \alpha$  (5)

The coefficient of restitution between  $P$  and the plane is  $e$ , where  $e > 0$

- (b) Show that  $v^2 = u^2(\sin^2 \alpha + e^2 \cos^2 \alpha)$  (3)

- (c) Show that the kinetic energy lost by  $P$  in the impact is

$$\frac{1}{2} mu^2(1 - e^2) \cos^2 \alpha \quad \text{(2)}$$

- (d) Hence find, in terms of  $m$ ,  $u$  and  $e$  **only**, the kinetic energy lost by  $P$  in the impact. (2)

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### Question 6 continued

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**Question 6 continued**

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Question 6 continued

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(Total for Question 6 is 12 marks)



7.

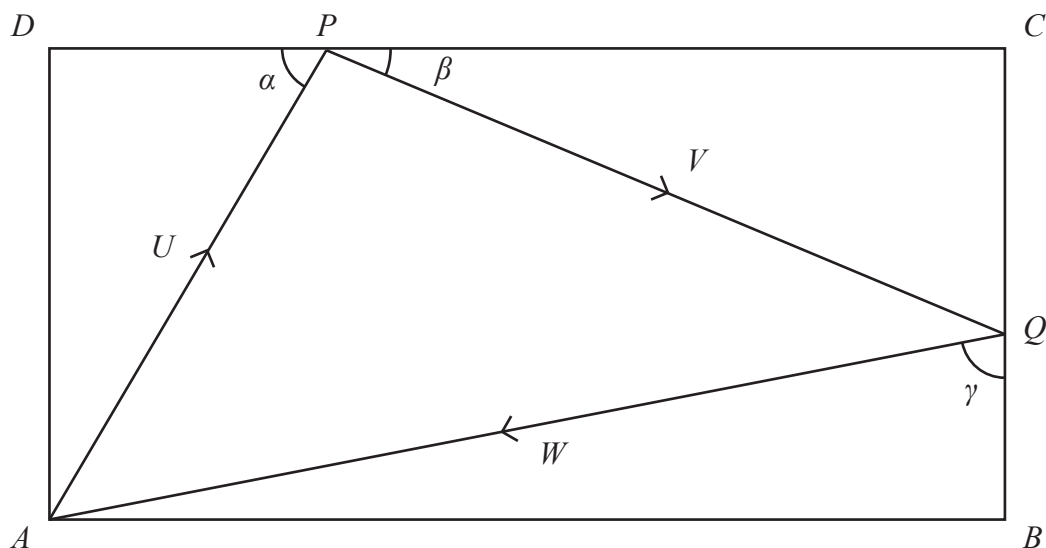


Figure 2

A small smooth snooker ball is projected from the corner  $A$  of a horizontal rectangular snooker table  $ABCD$ .

The ball is projected so it first hits the side  $DC$  at the point  $P$ , then hits the side  $CB$  at the point  $Q$  and then returns to  $A$ .

Angle  $APD = \alpha$ , Angle  $QPC = \beta$ , Angle  $AQB = \gamma$

The ball moves along  $AP$  with speed  $U$ , along  $PQ$  with speed  $V$  and along  $QA$  with speed  $W$ , as shown in Figure 2.

The coefficient of restitution between the ball and side  $DC$  is  $e_1$

The coefficient of restitution between the ball and side  $CB$  is  $e_2$

The ball is modelled as a particle.

**Use the model to answer all parts of this question.**

(a) Show that  $\tan \beta = e_1 \tan \alpha$  (4)

(b) Hence show that  $e_1 \tan \alpha = e_2 \cot \gamma$  (3)

(c) By considering (angle  $APQ +$  angle  $AQP$ ) or otherwise, show that it would be possible for the ball to return to  $A$  only if  $e_2 > e_1$  (6)

If instead  $e_1 = e_2$ , the ball would **not** return to  $A$ .

Given that  $e_1 = e_2$

(d) use the result from part (b) to describe the path of the ball after it hits  $CB$  at  $Q$ , explaining your answer. (1)





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### Question 7 continued

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Question 7 continued

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Question 7 continued

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Lined writing area for the answer to Question 7.



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**Question 7 continued**

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**(Total for Question 7 is 14 marks)**

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**TOTAL FOR PAPER IS 75 MARKS**

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