

Please check the examination details below before entering your candidate information

Candidate surname

Other names

Centre Number

Candidate Number

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Pearson Edexcel Level 3 GCE

Monday 5 June 2023

Afternoon (Time: 1 hour 30 minutes)

Paper
reference

9FM0/02

Further Mathematics

Advanced

PAPER 2: Core Pure Mathematics 2

You must have:

Mathematical Formulae and Statistical Tables (Green), calculator

Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebraic manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear.
Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 9 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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Question 4 continued

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Question 4 continued

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5. The points representing the complex numbers $z_1 = 35 - 25i$ and $z_2 = -29 + 39i$ are opposite vertices of a regular hexagon, H , in the complex plane.

The centre of H represents the complex number α

- (a) Show that $\alpha = 3 + 7i$ (2)

Given that $\beta = \frac{1+i}{64}$

- (b) show that

$$\beta(z_1 - \alpha) = 1 \quad (2)$$

The vertices of H are given by the roots of the equation

$$(\beta(z - \alpha))^6 = 1$$

- (c) (i) Write down the roots of the equation $w^6 = 1$ in the form $re^{i\theta}$ (1)

- (ii) Hence, or otherwise, determine the position of the other four vertices of H , giving your answers as complex numbers in Cartesian form. (4)



Question 5 continued

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Question 5 continued

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Question 5 continued

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(Total for Question 5 is 9 marks)



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6. Given that

$$y = e^{2x} \sinh x$$

prove by induction that for $n \in \mathbb{N}$

$$\frac{d^n y}{dx^n} = e^{2x} \left(\frac{3^n + 1}{2} \sinh x + \frac{3^n - 1}{2} \cosh x \right)$$

(6)

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Question 6 continued

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(Total for Question 6 is 6 marks)



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7.

In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

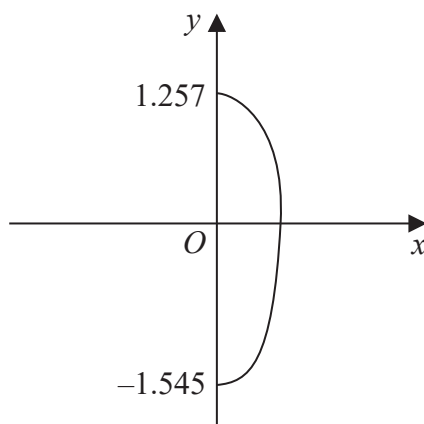


Figure 2

John picked 100 berries from a plant.

The largest berry picked was approximately 2.8 cm long.

The shape of this berry is modelled by rotating the curve with equation

$$16x^2 + 3y^2 - y \cos\left(\frac{5}{2}y\right) = 6 \quad x \geq 0$$

shown in Figure 2, about the y-axis through 2π radians, where the units are cm.

Given that the y intercepts of the curve are -1.545 and 1.257 to four significant figures,

- (a) use algebraic integration to determine, according to the model, the volume of this berry.

(6)

Given that the 100 berries John picked were then squeezed for juice,

- (b) use your answer to part (a) to decide whether, in reality, there is likely to be enough juice to fill a 200 cm^3 cup, giving a reason for your answer.

(2)



Question 7 continued

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Question 7 continued

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Question 7 continued

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(Total for Question 7 is 8 marks)



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8. Given that a cubic equation has three distinct roots that all lie on the same straight line in the complex plane,

(a) describe the possible lines the roots can lie on.

(2)

$$f(z) = 8z^3 + bz^2 + cz + d$$

where b , c and d are real constants.

The roots of $f(z)$ are distinct and lie on a straight line in the complex plane.

Given that one of the roots is $\frac{3}{2} + \frac{3}{2}i$

(b) state the other two roots of $f(z)$

(1)

$$g(z) = z^3 + Pz^2 + Qz + 12$$

where P and Q are real constants, has 3 distinct roots.

The roots of $g(z)$ lie on a different straight line in the complex plane than the roots of $f(z)$

Given that

- $f(z)$ and $g(z)$ have one root in common
- one of the roots of $g(z)$ is -4

(c) (i) write down the value of the common root,

(1)

(ii) determine the value of the other root of $g(z)$

(3)

(d) Hence solve the equation $f(z) = g(z)$

(4)



Question 8 continued

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9. A patient is treated by administering an antibiotic intravenously at a constant rate for some time.

Initially there is none of the antibiotic in the patient.

At time t minutes after treatment began

- the concentration of the antibiotic in the blood of the patient is x mg/ml
- the concentration of the antibiotic in the tissue of the patient is y mg/ml

The concentration of antibiotic in the patient is modelled by the equations

$$\frac{dx}{dt} = 0.025y - 0.045x + 2$$

$$\frac{dy}{dt} = 0.032x - 0.025y$$

- (a) Show that

$$40\,000 \frac{d^2y}{dt^2} + 2800 \frac{dy}{dt} + 13y = 2560 \quad (3)$$

- (b) Determine, according to the model, a general solution for the concentration of the antibiotic in the patient's tissue at time t minutes after treatment began. (5)
- (c) Hence determine a particular solution for the concentration of the antibiotic in the tissue at time t minutes after treatment began. (4)

To be effective for the patient the concentration of antibiotic in the tissue must eventually reach a level between 185 mg/ml and 200 mg/ml.

- (d) Determine whether the rate of administration of the antibiotic is effective for the patient, giving a reason for your answer. (2)



Question 9 continued

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Question 9 continued

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(Total for Question 9 is 14 marks)

TOTAL FOR PAPER IS 75 MARKS

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